

Math 210-1, ANSWERS to SAMPLE FINAL EXAMINATION, Fall 2002

1. Please see your textbook.
2. The right-hand column has four T's; simplified statement: T; the corresponding circuit has no switches, this is just a solid line on the picture.
3. $n(A \cup B) = 48$. 4. $7/12$. 5. $7/27$. 6. 1728. 7. 220.
8. $C(5, 3) \cdot C(6, 4)/C(18, 7) = 25/5304$. 9. $-\$.40$ 10. .0918
11. The mean is 5.67; the standard deviation $s = \sqrt{33.22}$.
12. $(x, y) = (x, (2x - 4)/3)$.
13. $(x, y, z) = (2.2, 1.2, 3.4)$. If you do not like decimals or fractions, try to solve the following problem:
$$\begin{aligned} 2x - y + 2z &= 10 \\ x + 2y + 3z &= 6 \\ 3x - y - z &= 2 \end{aligned}$$

(This system has integer solutions, do not forget to check your answer!)
14. $AB = \begin{pmatrix} -3 & -4 & -9 \\ 9 & 2 & 2 \end{pmatrix}$; BA does not exist.
15. Max $z = 18$ at $(1, 3)$.
16. x is the number of cocktail tables;
 y is the number of end tables;
 z is the objective function (profit).
Maximize $z = 12x + 10y$
subject to: $2x + 4y \leq 20$
 $3x + y \leq 15$
 $x \geq 0$
 $y \geq 0$.
17. (a) No dominated strategies; 2 is a saddle point; the game is strictly determined. The optimum strategies: $(0, 1, 0)$ for player A and $(1, 0, 0)$ for player B. The value of the game is 2, so it is not fair.
(b) Dominated strategies: row 3 and columns 3 and 4. No saddle points, so the game is not strictly determined. The optimum strategies: $(1/3, 2/3, 0)$ for player A and $(2/3, 1/3, 0, 0)$ for player B. The value of the game is $-2/3$, so it is not fair.